



**INFLUENCE OF PIEZOELECTRIC MATERIAL ON CANTILEVER PLATE
NATURAL FREQUENCIES**

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ARTICLE INFO

Article History:

Received 11th January, 2017

Received in revised form 19th February, 2017

Accepted 22nd March, 2017

Published online 28th April, 2017

Key words:

Cantilever plate, piezoelectric patch, Modal analysis, Natural frequencies.

ABSTRACT

This paper presents the modal analysis of cantilever plate with and without piezoelectric patch by using Finite Element Analysis (Ansys) software. A modal analysis was carried out on cantilever plate having piezoelectric patch at 6 different locations. By comparison we observed that natural frequency of plate was increased with first 2 locations of PZT patch and natural frequency was decreased with next 4 locations of PZT patch. PZT patch is used due to it Direct Piezoelectric Effect with which we can sense the physical deformation of the plate, in turn this plate can be used in sensing of deformations of different objects with which it is attached to.

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INTRODUCTION

Piezoelectricity is the ability of a material to develop an electric charge when subjected to a mechanical strain, this effect is called Direct Piezoelectric Effect (DPE) and Conversely material develop mechanical strain in response to an applied electric field, this effect is called Converse Piezoelectric Effect (CPE). Due to this coupled mechanical and electrical properties, piezoelectric materials make them well suited for use as sensors and actuators. Sensors use Direct Piezoelectric Effect (DPE) and actuators use Converse Piezoelectric Effect (CPE). As a sensors, deformations cause by the dynamic host structure produce an electric change resulting in an electric current in the sensing circuit. While as an actuators, a high voltage signal is applied to piezoelectric device which deforms the actuator and transmit mechanical energy to the host structure. Piezoelectric materials basically divided into two group Piezo-ceramics and piezo-polymers. Lead (plumbum) Zirconate Titanate (PZT) became the dominant piezo-electric ceramic material for transducer due to its high coupling coefficient (0.65). When this PZT plate subjected to static or dynamic loads, it can generate voltages as high as 20,000 volts. A steel cantilever plate is considered for the modal analysis coupled with PZT (Lead (Plumbum) Zirconate Titanate) at different positions.

System Model

A cantilever plate is designed in Ansys with dimensions mentioned below in table.

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Table 1 Properties of cantilever plate

Thickness b	0.03 m
Height h	0.002m
Length from fixed end L	0.11 m
Young's modulus E	207x109 N/m2
Density ρ	7800 kg/m3
Poisson ratio μ	0.3
Density ρ of piezoelectric material	7800kg/m3
Piezo patch dimensions(l*b*h)	0.02m*0.01m*0.002m

Table 2 Anisotropic Properties

Linear Elastic Anisotropic properties(N/m ³)	
D11	1.26*1011
D12	8.41*1010
D13	7.95*1010
D22	1.17*1011
D23	8.41*1010
D33	1.2*1011
D44	2.3*1010
D55	2.3*1010
D66	2.35*1010

Table 3 Electromagnetic Properties

Electromagnetic Relative Permittivity(F/m)	
ε ₁₁	1.151*10 ⁻³
ε ₂₂	1.043*10 ⁻³
ε ₃₃	1.151*10 ⁻³

Table 4 Piezoelectric Properties

Piezoelectric constant stress matrix(C/m ²)	
e ₁₂	-5.4
e ₂₂	15.8
e ₃₂	-5.4
e ₄₁	12.3
e ₅₃	12.3

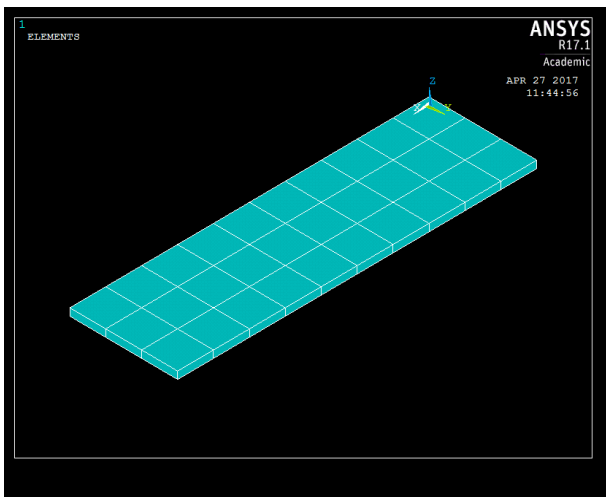


Fig 1 Cantilever Plate without PZT patches.

In ANSYS, the plate is modelled using a solid186 element and the PZT's are modelled using a 3-D coupled element (SOLID226). The actuator is placed in six different positions as shown in Fig [2.2- 2.7]. Note that each square is 0.01 x 0.01 m in size.

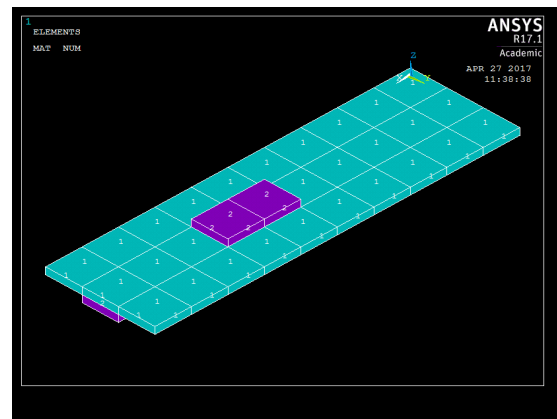


Fig 4 Cantilever Plate with PZT patches at Position-3

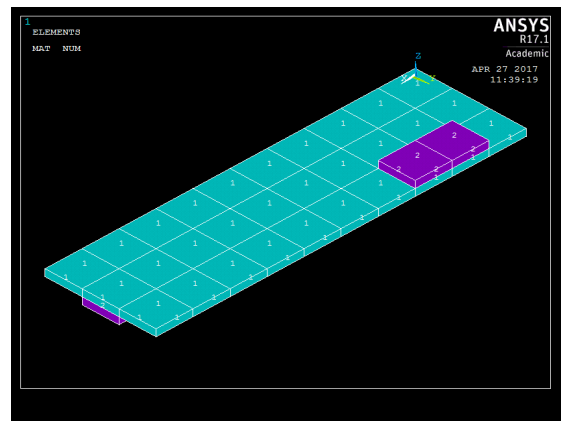


Fig 5 Cantilever Plate with PZT patches at Position-4

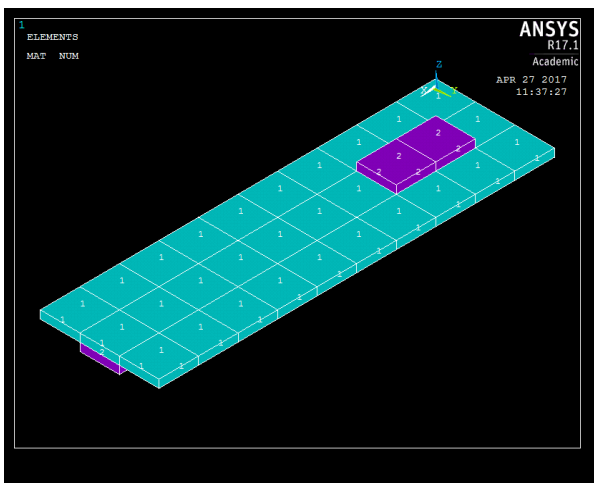


Fig 2 Cantilever Plate with PZT patches at Position-1

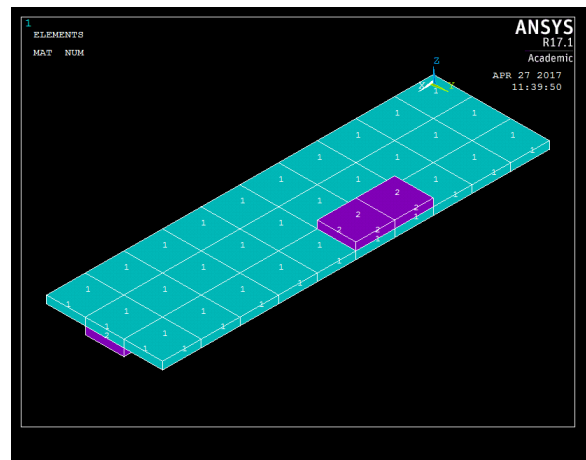


Fig 6 Cantilever Plate with PZT patches at Position-5

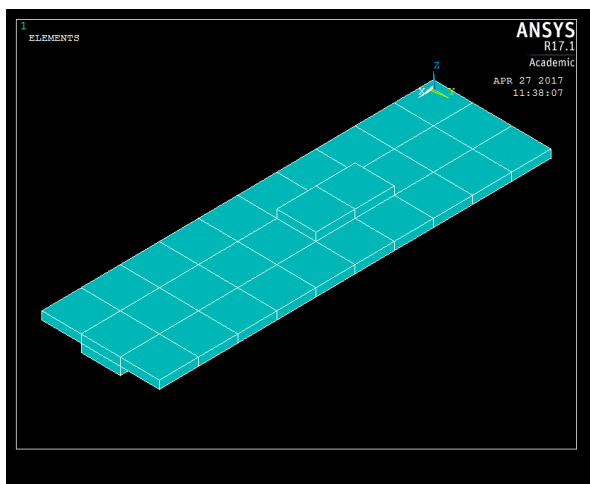


Fig 3 Cantilever Plate with PZT patches at Position-2

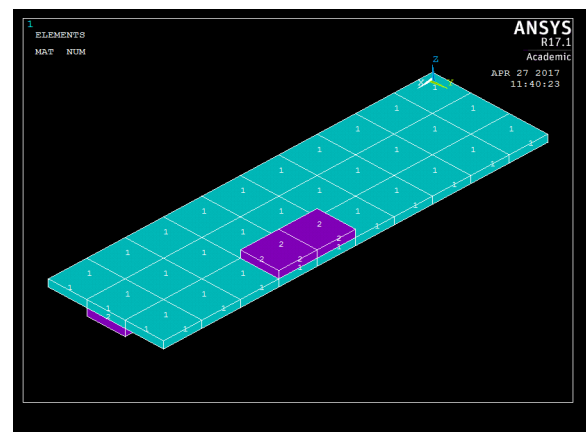


Fig 7 Cantilever Plate with PZT patches at Position-6.

Previous Work

Boucher et al developed a perturbation method to numerically determine the Eigen modes of vibration for piezoelectric transducers. The three-dimensional finite element method was formulated to predict the piezoelectric transducer resonance and anti-resonance frequencies as well as sound radiation for different sizes of the PZT cubes. Ha et al modeled laminated composite structures containing distributed piezoelectric ceramic sensors and actuators by finite element analysis. The computer code was developed to analyze the mechanical-electrical response of the piezoelectric ceramic laminated composites. Experiments were also conducted to verify the computer simulations. The comparisons between predicted and experimental results agreed well. Sun et al derived the frequency response function (FRF) through electric admittance of piezoelectric transducers for obtaining the dynamic parameters of beam structures. However, they did not physically interpret those dynamic parameters.

Proposed Methodology

Cantilever plate was modeled and properties of steel were assigned to that model. Model analysis was done on plane plate. Piezoelectric material was placed on the plate at 6 different positions and model analysis was carried on. Obtained results were compared with each other arrived with a conclusion for the best position of piezoelectric material.

Simulation Results

Vibration behavior of a cantilever plate simulated in FEA software ANSYS.

The natural frequencies are obtained when the PZT patch is placed on cantilever plate at different positions compared to the natural frequencies of the plate without PZT patches as indicated in the figure5.1 to figure5.32.

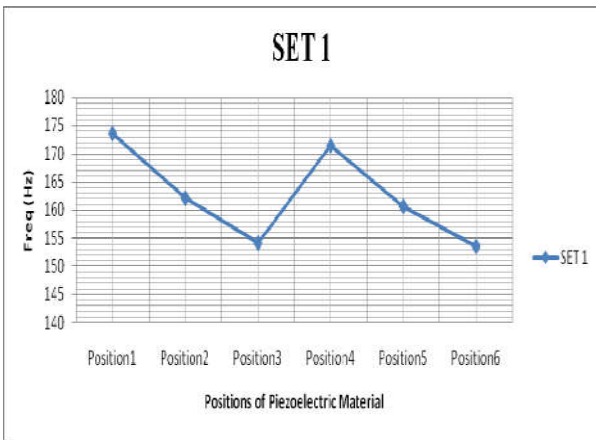


Fig 1 Set 1 Frequencies at different positions.

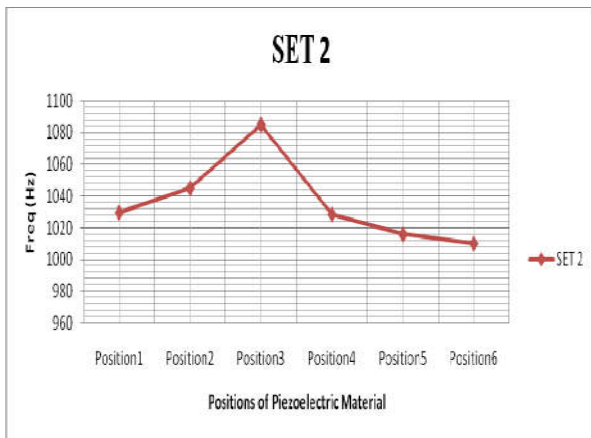


Fig 2 Set 2 Frequencies at different positions.

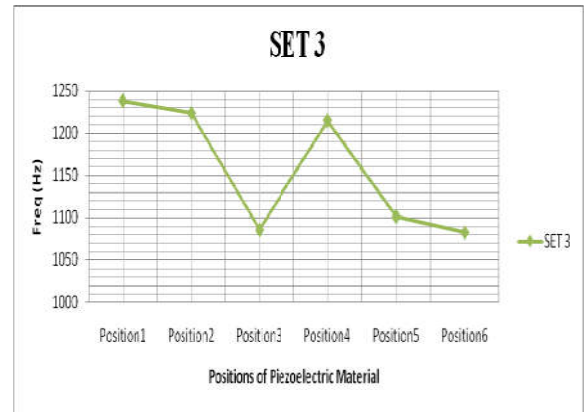


Fig 3 Set 3 Frequencies at different positions

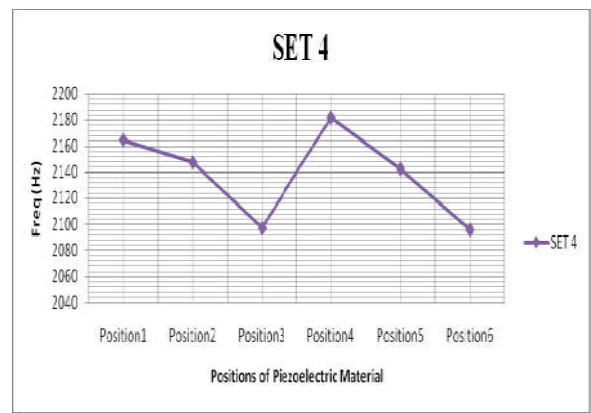


Fig 4 Set 4 Frequencies at different positions

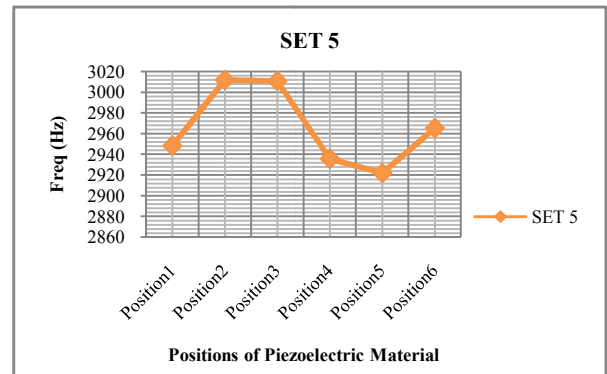


Fig 5 Set 5 Frequencies at different positions

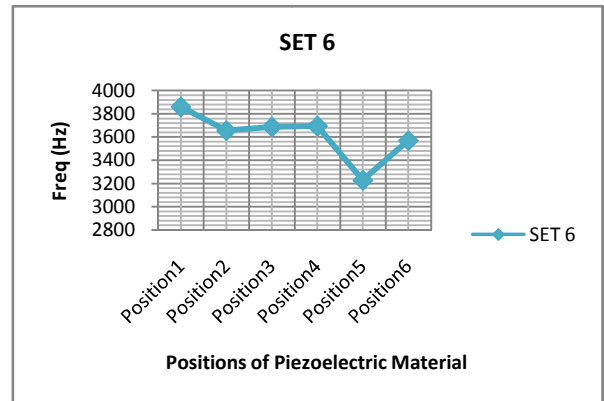


Fig 6 Set 6 Frequencies at different positions.

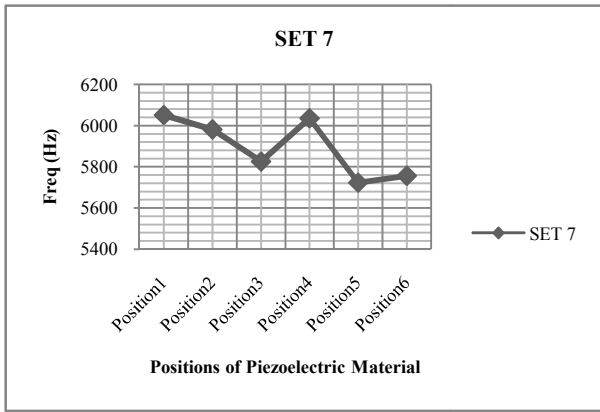


Fig 7 Set 7 Frequencies at different positions

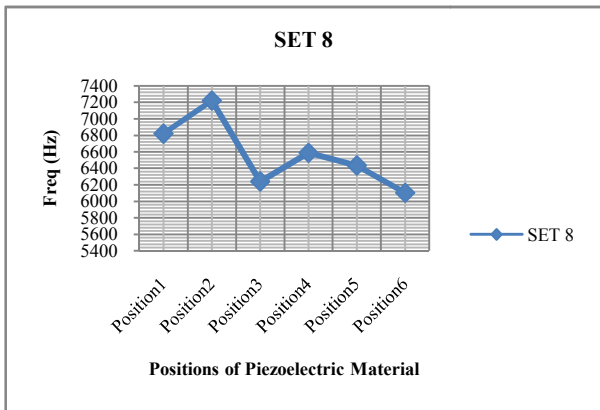


Fig 8 Set 8 Frequencies at different positions

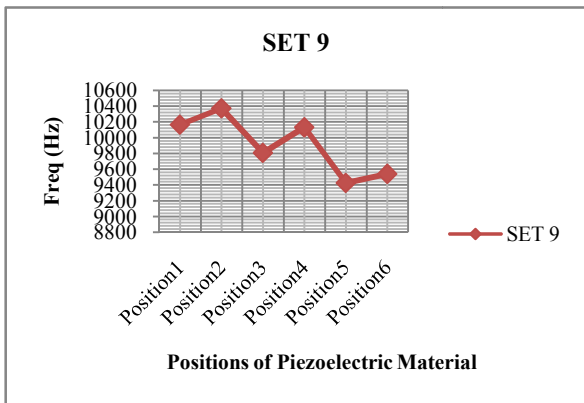


Fig 9 Set 9 Frequencies at different positions

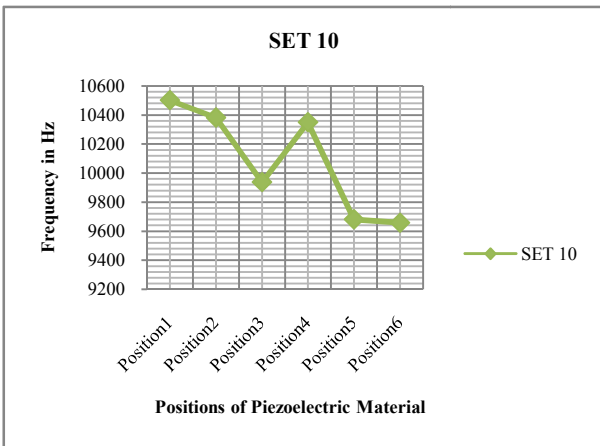


Fig 10 Set 10 Frequencies at different positions.

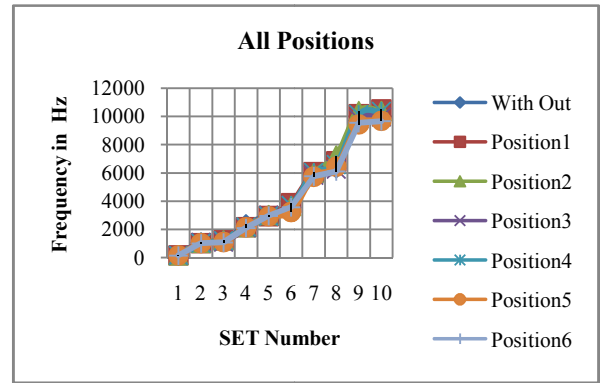


Fig 11 Sets Vs Positions

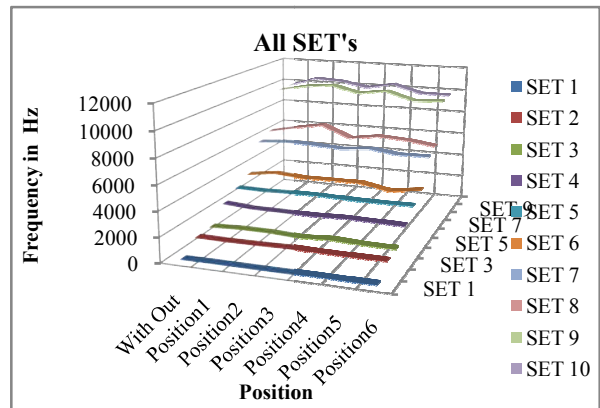


Fig 12 Sets Vs Positions in 3D

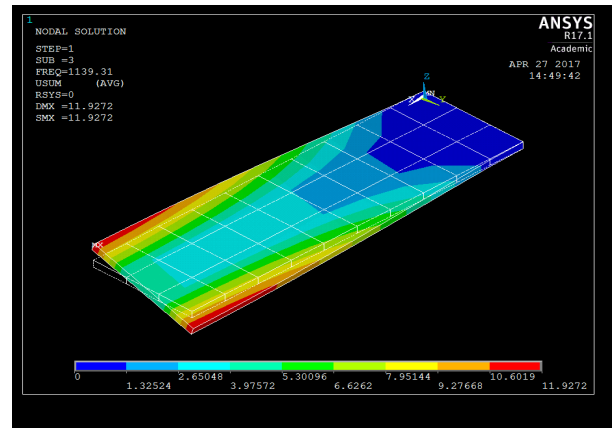


Fig 13 Set 3 Deformation plot of plane plate.

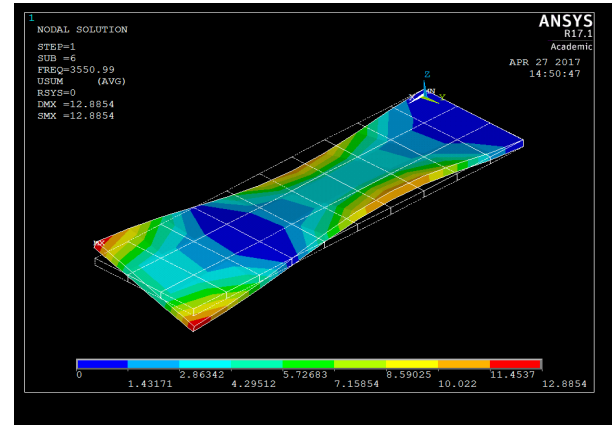


Fig 14 Set 6 Deformation plot of plane plate.

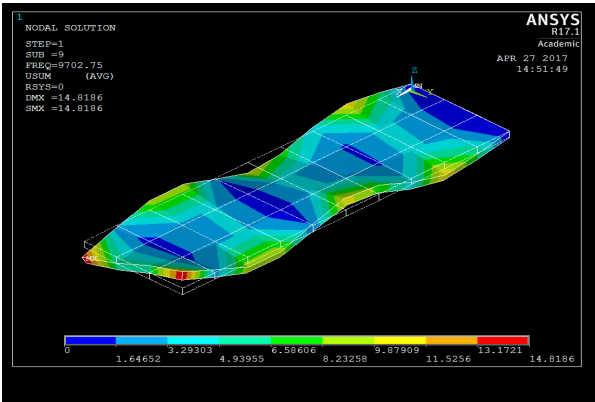


Fig 15 Set 9 Deformation plot of plane plate

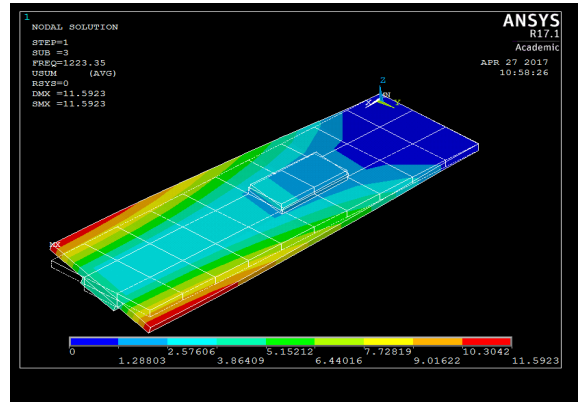


Fig 19 Set 3 Deformation plot of PZT plate at position 2

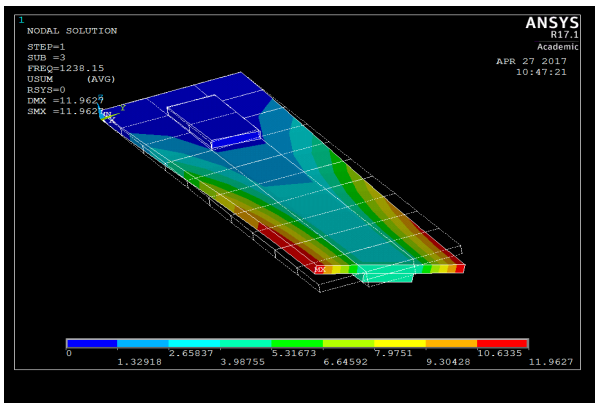


Fig 16 Set 3 Deformation plot of PZT plate at position 1

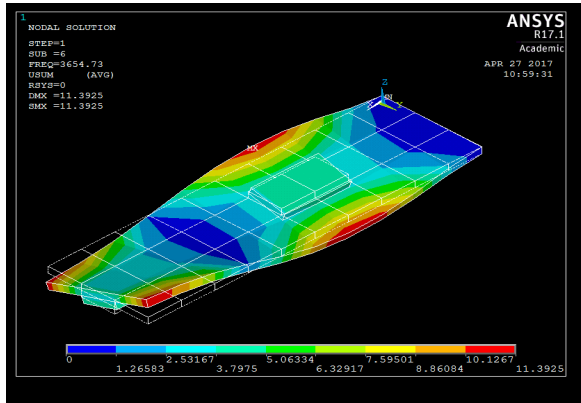


Fig 20 Set 6 Deformation plot of PZT plate at position 2

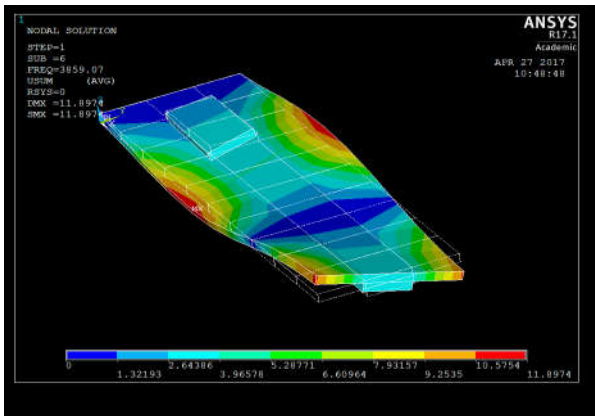


Fig 17 Set 6 Deformation plot of PZT plate at position 1

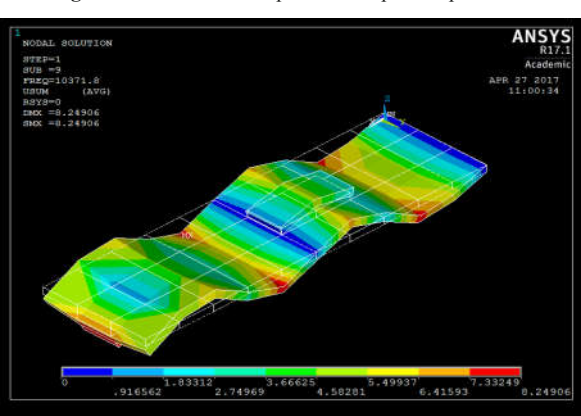


Fig 21 Set 9 Deformation plot of PZT plate at position 2

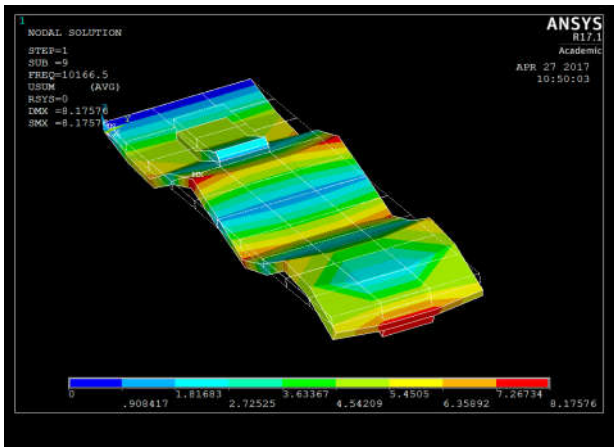


Fig 18 Set 9 Deformation plot of PZT plate at position 1

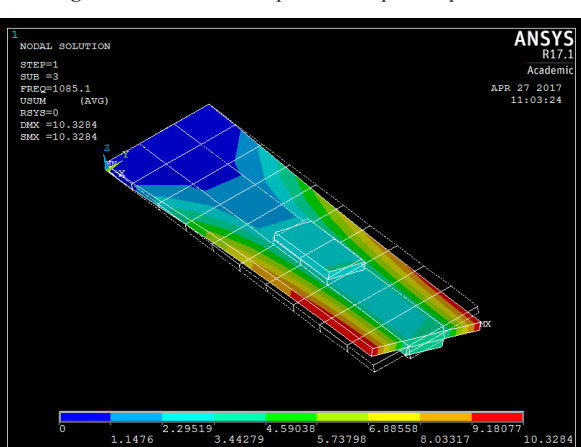


Fig 21 Set 3 Deformation plot of PZT plate at position 3

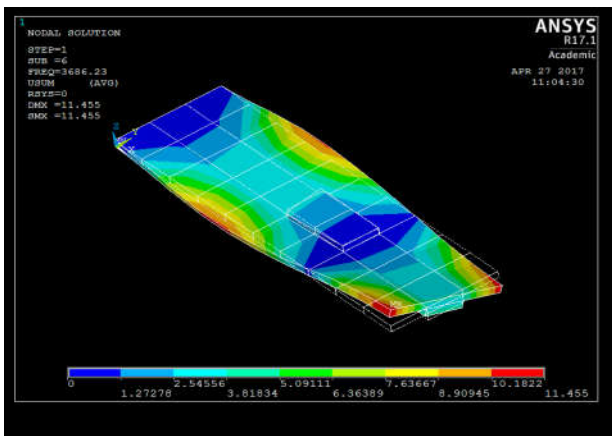


Fig 22 Set 6 Deformation plot of PZT plate at position 3

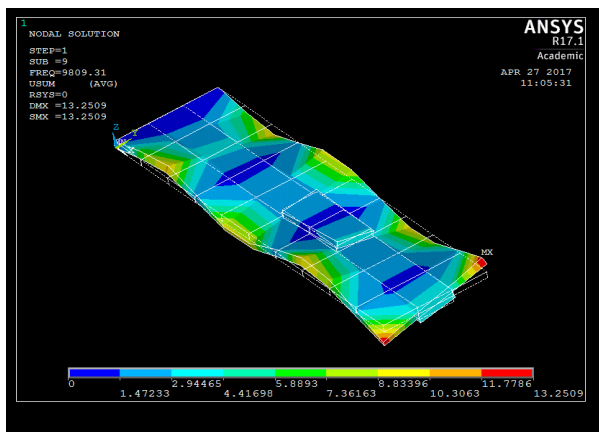


Fig 23 Set 9 Deformation plot of PZT plate at position 3

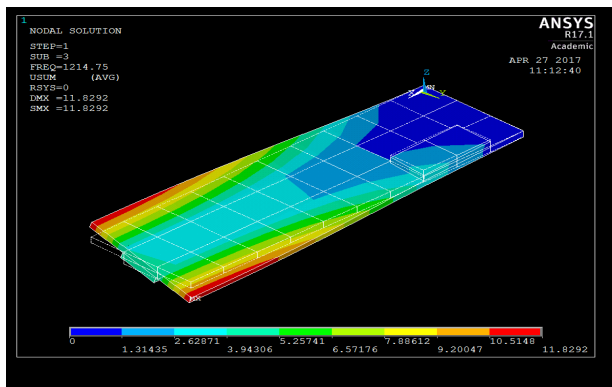


Fig 24 Set 3 Deformation plot of PZT plate at position 4

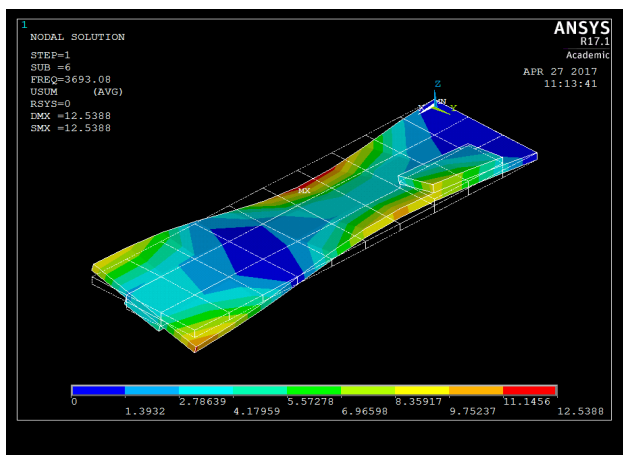


Fig 25 Set 6 Deformation plot of PZT plate at position 4

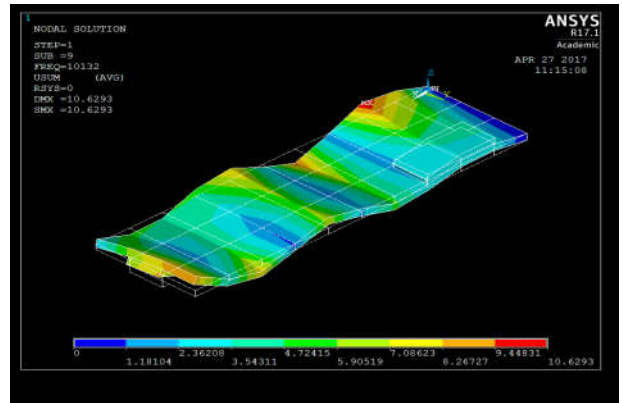


Fig 26 Set 9 Deformation plot of PZT plate at position 4

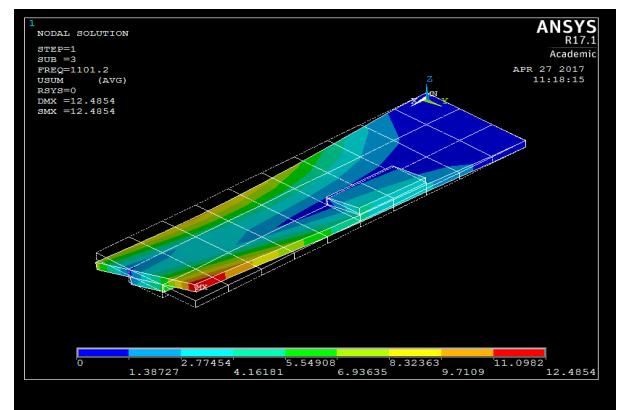


Fig 27 Set 3 Deformation plot of PZT plate at position 5

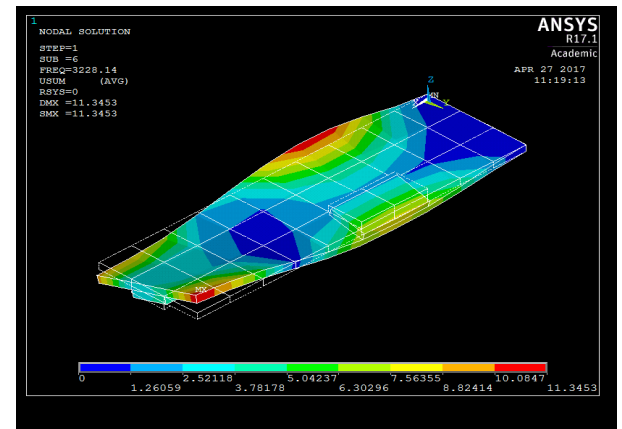


Fig 28 Set 6 Deformation plot of PZT plate at position 5

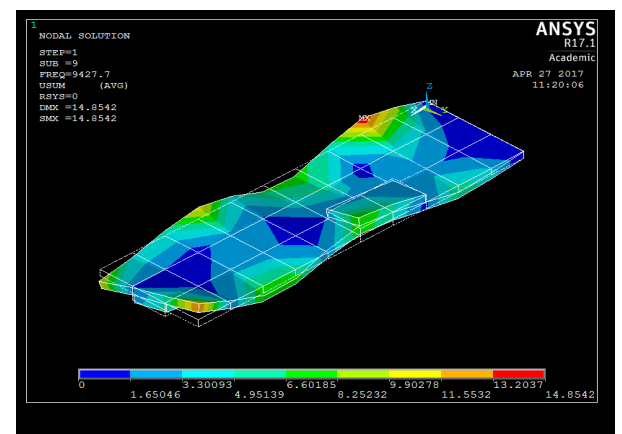


Fig 29 Set 9 Deformation plot of PZT plate at position 5

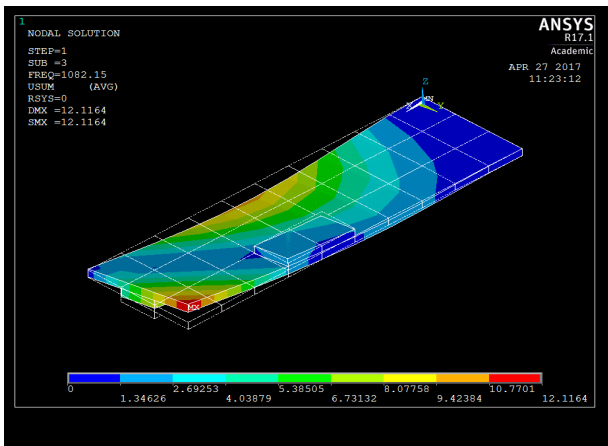


Fig 30 Set 3 Deformation plot of PZT plate at position 6

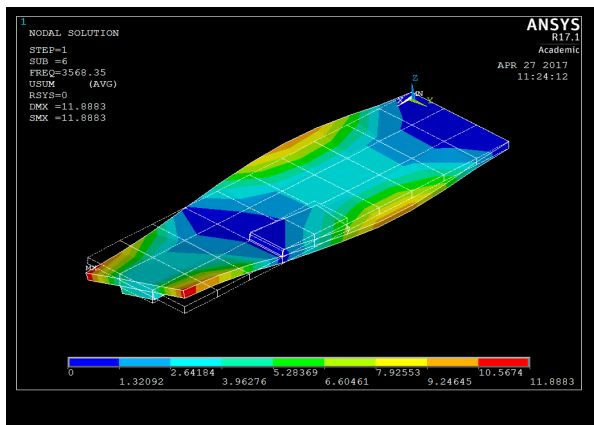


Fig 31 Set 6 Deformation plot of PZT plate at position 6

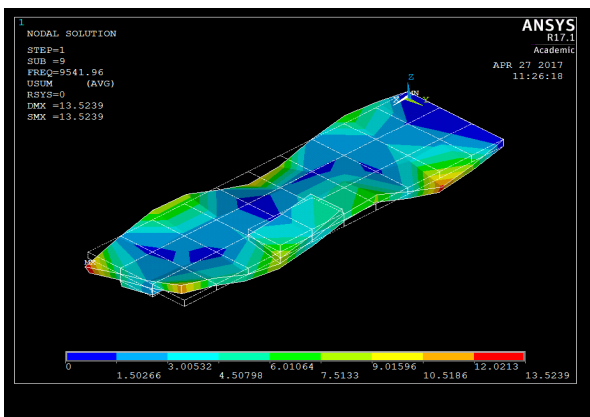


Fig 32 Set 9 Deformation plot of PZT plate at position 6

S.No	With Out	Position 1	Position 2	Position 3	Position 4	Position 5	Position 6
1	170.99	173.54	162.08	154.06	171.38	160.6	153.49
2	1067.6	1029.5	1044.9	1084.9	1028.4	1015.8	1010
3	1139.3	1238.1	1223.4	1085.1	1214.7	1101.2	1082.1
4	2352.6	2164.4	2147.3	2097.2	2181.6	2142.4	2095.9
5	2992	2948.3	3011.8	3010.7	2935.7	2922	2965.3
6	3551	3859.1	3654.7	3686.2	3693.1	3228.1	3568.4
7	5873.6	6051.3	5981.9	5825.9	6035.8	5723.2	5756.4
8	6338.7	6820.3	7220.9	6240.7	6588.6	6434.3	6103.1
9	9702.7	10166	10372	9809.3	10132	9427.7	9542
10	9718.2	10502	10382	9937.8	10350	9681.3	9658.5

CONCLUSION

Vibration behavior of the cantilever plate was observed as follows. Frequencies of without and with PZT patch at SET's 1, 2 and 3 were close to each other and did not showed any significant change. When we reach SET's 4, 5 and 6 there was

slight increase in frequencies. For SET's of 7, 8, 9 and 10 there was a drastic change in frequencies.

Surprisingly for positions 1 and 2 the natural frequency of plate was more when compared to without PZT (plane) plate. For positions of 3, 4, 5 and 6 the natural frequencies were reduced comparatively.

Future Scopes

In future, the application of PZT actuators for the Composite smart structures can be carried out.

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