



DEVELOPMENT OF A COURSE ASSESSMENT PROTOTYPE REAL ANALYSIS THROUGH RMT (RIGOROUS MATHEMATICAL THINKING) APPROACH BASED ON GENDER

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ABSTRACT

This study uses Research and Development (RnD) method with the aim of looking at the assessment sheet that has existed so far, developing a prototype assessment of the Real Analysis subject, and testing its validity, reliability and effectiveness. Development of assessment prototypes refers to the Borg and Gall model. The assessment prototype consists of RMT ability test and a Real Analysis course assessment instrument designed to measure the subject cognitive domain with the RMT approach, and adjusted to the style of thinking according to gender. The technique of collecting data is by giving written tests for material in the real function line, followed by documentation, observation, interviews, and questionnaires. The initial product data analysis is validated by experts to obtain content validity. Furthermore, the instrument is tested on a limited basis to subjects who contracted 15 Real Analysis courses. The results of the trial assessment instrument with the RMT approach are measured by the product moment formula, while the reliability test uses alpha formula. The difficulty level of the test questions for the ability of the RMT and the distinguishing power are also measured. In the assessment instrument with the RMT approach adjusted to the subject's thinking style based on gender, the validity and reliability are measured. The results show that the Real Analysis course assessment instrument through a gender-based RMT approach that has been developed is valid, reliable, practical and effective.

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INTRODUCTION

Assessment instruments development is one of the efforts to improve academic quality and subject learning achievement (in this case students). Before the assessment instrument is implemented, an analysis of the subject's learning needs and situations is carried out first. Then, it is so tested for its validity, practicality and effectiveness that produces an assessment product that can be useful for lecturers and subjects. The problems now is the assessment instruments in an educational institution are not optimally developed. So far, almost all assessments of lectures are only centered on the results of midterm (UTS), final examinations (UAS), and structural and independent assignments. However, these personal assessment indicators are not so well cared that lecturers are not able to assess objectively. This is in line with the opinion (James Beyers, 2011) which says that educators should make a structured and personal assessment system for students that starts from the maturity process in thinking mathematically so that it will look more just and wise. In addition, Muhammad.

YM (2018) explained that the scoring system should pay attention to the mathematical mindset of the subject and one of these can be seen from his or her thinking habits according to gender.

The increase in rigor mathematical thinking (RMT) ability of the subject is closely related to the intelligence level both intellect and emotional. According to Firmasari & Sulaiman (2019) stated that "subjects with low cognitive categories have not been systematic and not thorough in solving mathematical problems." It is known that individual intelligence is largely determined by the work of the brain. This is confirmed by the statement (Evania, 2011) that "brain development is closely related to the development of the prefrontal cortex which requires the longest time than other brain regions". So that it becomes the main responsibility in developing the RMT. Thus, learning activities during lectures must pay attention to brain function and performance. This is again reinforced by a statement (Jensen.TS, 2012) namely "the brain is involved in everything we do in school, so if we ignore it, it means we are not responsible". One of the results of the research explained that "In particular, my position was (and still is) that the cognitive and brain system that have evolved to enable movement in and the representation of three-dimensional space are more highly elaborated in boys and men than in girls and women" (Geary, 1998). Geary revealed that three-

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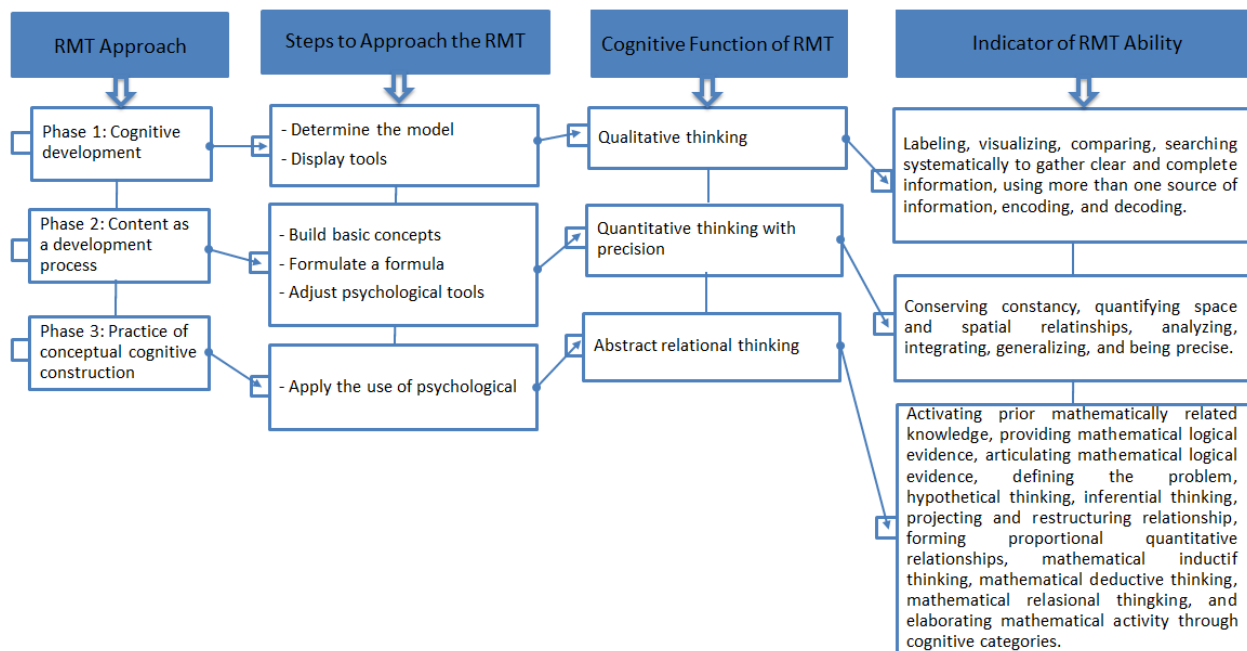
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dimensional spatial abilities of men are better or faster than women. Furthermore, this study shows that women learn differently from men because of their abilities and different ways of thinking. According to Firmasari et al, (2019) the confidence of male students in mathematical abilities is higher than that of women.

Nurhayati (2017) states that differences in intellectual abilities between women and men include three things, namely: (1) verbal ability, (2) visual-spatial ability, and (3) mathematical ability. Women have oral ability better than boys, boys excel in visual-spatial and mathematical abilities. Alifah (2012) summarized the differences in abilities between men and women based on expert opinion in the form of the table below.

Table 1 Differences in Cognitive Ability between Men and Women in the Opinion of Experts

Research Resources	Talent and Interest	
	Male	Female
University of Cambridge	mechanical motion, *good gross motoric*, not easy to express fear, and more emotional.	a reliable imilator, superior hand ability, tends to be timid, and not easily emotional.
MichaelGurian	has a brain that tends to develop and has a more complex spatial, verbal ability that is 7,000 words per day, does not contain serotonin and aksitosin in the brain, brain size is smaller than women.	have less spatial ability, high verbal ability which is about 20,000 words per day, contains serotonin and aksitosin in the brain which makes him calm and understand other people, and has a larger brain size.
Macooby dan Jacklin	the verbal abilities period is low, but will be about the same age of 11 years, spatial visual abilities are superior in teenagers.	the verbal ability period is high, and low spatial visual abilities in teenagers.
Ward	likethe field of physics.	underachieving in mathematics and preferring biology.
Dweck	experimenting	refuse to take risks in experimenting.
Cameron	master the shadow of more complex shapes.	women lack mastery in the shadow of more complex forms.



Picture 1 Chart of the relationship between the RMT approach and the RMT ability (Kinard, 2015)

Based on the background of the problems stated above, it is necessary to develop a assessment prototype with a RMT approach based on gender that is able to represent each thinking style of the two different sexes. The ability development of the RMT is very necessary so that the subject understands the concepts learned and to exercise sharpness, critical power and can develop and improve the subject's high-level thinking skills (Yunitadkk, 2018). It is very important to know the RMT's capabilities because it requires a valid and reliable assessment instrument. Rigorous Mathematical Thinking (RMT) according to Kinard, (2007) "The RMT invention defines mathematical rigor as that quality of thought that reveals itself when learners are engaged through a state of

vigilance – driven by a strong, persistent, and inflexible desire to know and deeply understand." The real analysis course is a very suitable course for applying the RMT because it contains compatible indicators with the RMT. To be clearer, the following is a chart of the relationship between the RMT approach and the RMT ability.

From the picture above, it can be seen that the RMT approach can be closely related to the RMT ability indicator. This can be seen from the thinking process of the subject which begins with the RMT approach and ends with an indicator of the ability of the RMT.

From this indicator, a Real Analysis course assessment instrument is prepared which is adjusted to the subject's cognitive thinking style according to gender. Thus the objectives of this study are (1) to make an assessment prototype for the Real Analysis course, (2) to design the Real Analysis course assessment instrument, (3) validate the results of the assessment instruments by expert validators, and (4) test the effectiveness and practicality of assessment instruments for the Real Analysis course that have been compiled. Therefore, the product produced from this study is a valid, practical and effective course assessment instrument sheet for Real Analysis.

LITERATURE REVIEW

RMT (Rigorous Mathematical Thinking)

RMT (Rigorous Mathematical Thinking) are first coined by James T. Kinard. According to Kinard (2007: 3) "The RMT invention defines mathematical rigor as that quality of thought that reveals itself when learners are engaged through a state of vigilance – driven by a strong, persistent, and inflexible desire to know and deeply understand." In here, RMT defines accuracy in mathematics, when students are involved in complex problems, students are driven by a strong desire, persistence, and an understanding concepts to understand problems. In thinking naturally involves the presence of cognitive functions, according to Meilantifa et al(2018: 2) cognitive function is a mental process that has special meaning conveyed for certain thinking actions needed to describe abstractions and generalize geometry directly. According to Kinard (2007: 4) for rigorous mathematical thinking three cognitive function levels are needed, namely level 1 (qualitative thinking), level 2 (quantitative thinking with accuracy), and level 3 (abstract relational thinking). According to FitriyanidanKhasanah (2017: 2) these three levels of cognitive function define mental processes of general cognitive skills to a higher level of mathematical knowledge. The RMT theory is based on two learning theories, namely socio-cultural Vygotsky whose emphasis is on his psychological equipment and mediated learning theory (Mediated Learning Experience or MLE) which was coined by ReuvanFeurstein. But the focus of this study is only on identifying students' ability to think mathematically in solving mathematical problems, not learning designs that involve intervention in RMT.

According to Pertiwi (2016: 106) there is a difference between mathematical thinking and rigor mathematical thinking where mathematical rigor thinking requires a higher level of precision and accuracy as well as more structured specific cognitive functions. According to Sumarmo in Fitriyani and Khasanah (2017: 1) "defined mathematical thinking as a way of thinking with regard to the process of math (doing math) or in solving mathematical tasks both simple and complex." According to Fitriati and Sopiana (2015: 46) in thinking rigor mathematically students have begun to realize the importance of the accuracy of the basic principles underlying a proof. Students can apply axioms, theorems, definitions and mathematical concepts that are appropriate for completing a proof. Students reason according to concepts in the mathematical system and can analyze the consequences of the axiom manipulation of theorems and definitions for proof, can understand the relationship between forms that are not defined, can solve mathematical problems in accordance with the rules or concepts that are right (Sholihah and Afriansyah, 2017 : 291).

In this research, Rigorous Mathematical Thinking is a high-level thinking skill that involves several cognitive functions. It requires an abstract and complicated thinking stage, students can determine and apply the right concepts to solve problems. Rigor is also often referred to as accuracy, and in mathematical thinking accuracy and logic are also needed, while according to Kinard the requirement to be precise and logical is the existence of rigorous, so rigorous mathematical thinking is needed in learning and solving mathematical problems. The development of Rigorous Mathematical Thinking skill is

indispensable so that students better understand the concepts learned and can apply them in various situations, to train students 'sharpness in focus, perception, critical power and can develop and improve students' high-level thinking skills. Because accuracy is the highest stage in understanding geometry.

According to Fitriyani and Khasanah (2017: 3) the RMT process requires the use of cognitive function from low-level to high-level cognitive functions. Mathematically-specific cognitive functions is specific thinking actions that are needed to deal directly with the abstractions and generalizations of mathematical stimuli" (Kinard, 2007: 4).

Prototype Assessment

Specifically in education Gronlund & Linn (Suprananto, 2012: 7) defines assessment as "a systemic process and includes the activities of collecting, analyzing, and interpreting information to determine how far a student or group of students achieves set learning goals, both aspects of knowledge, attitude, and skill." According to Nitko (1996) assessment is a process that is taken to obtain information used in order to make decisions regarding students, curriculum, programs, and education policies, methods and or other educational instruments by an agency, the institution that organizes a certain activities. According to Suwandi (2010: 7) assessment is "a process to know whether the process and results of an activity program are in accordance with the objectives or criteria that have been set." Based on the above understanding it can be concluded that assessment is a systematic process and includes the activities of collecting, analyzing, and interpreting information to know whether the process and results of an activity program are in accordance with the objectives or criteria that have been set. Where the assessment is not separate from the measurement process.

Habits of Gender-Based Mathematical Thinking

In essence, all beings are created in pairs. In humans, for example, there are men and women. Both are created in the same degree, dignity and dignity. Even if they have different forms and functions, they are all so that they complement each other. However, in the course of human life, there are many changes in the roles and status of both, especially in society. The process has gradually become habitual and cultured which has the potential to result in discrimination against one sex in the community. Gender is an English word absorption. Gender is a basic element of self-concept. Knowledge "I am a woman" or "I am a man" is one of the core parts of our personal identity (David O. Sears, Jonathan L. Freedman and L. Anne Peplau, 2005). The term "gender" is stated by social scientists with the intention of explaining the differences between women and men who have innate traits (god creation) and cultural formations (social construction). Often people mix up human characteristics that are natural (unchanging) with those that are non-natural (gender) that can change and be changed. This difference in gender roles also makes people think again about the division of roles that are considered inherent in both women and men.

Gender differences are one of a variety of differences that exist in the classroom. Male and female students have differences in several ways. Elliott (2000) has revealed several differences in students in terms of gender differences. The obvious difference

is the physical difference. Boys usually have a bigger and stronger physique even though almost all girls mature faster than boys. Boys are also said to be superior in terms of spatial skills than girls. Even so, boys often experience problems in terms of language, so girls are declared superior in terms of verbal abilities. This gender difference also seems to influence the amount of motivation of students to achieve. This is because of the assumption that boys are superior in the fields of science and mathematics, while girls will be superior to more feminine tasks such as art and music. The next difference is the level of aggressiveness, boys tend to be more aggressive than girls. Boys and girls are different, and as a result, differences arise about how they learn. For example, Orhun (in Trisniawati, 2013) investigated the relationship between gender and learning styles. The results show that there are differences between learning styles that are preferred by male and female students. The study found that female students preferred convergent learning styles. Convergent dominant learning ability uses abstract conceptualization and active experimentation. Students with this learning style prefer inquiry type discovery. While most male students in this study preferred the assimilator learning style. Dominant learning ability assimilators use abstract conceptualization and reflection observation. They learn by seeing and thinking. Some studies to examine how gender differences relate to mathematics learning, men and women are compared using variables including innate abilities, attitudes, motivations, talents, and performance (Good child & Granholm in Trisniawati, 2013). Some researchers believe that the influence of gender factors (the influence of male and female differences) in mathematics is due to biological differences in the brains of boys and girls that are known through observation, that girls, in general, are superior in the field of language and writing, while boys are superior in the field of mathematics, because of their better spatial abilities (Geary, Sauls, Liu, in Trisniawati, 2013).

As a result, gender differences in mathematics are quite difficult to change. However, on the other hand, various studies state that there is no role for gender, male or female, that excels in each other in mathematics and in the end, women can be superior in various fields related to mathematics. Various studies have found that gender differences influence mathematics learning. This occurs during elementary school age. Another study states that the influence of gender differences can be observed in junior high school students and in high school students. In high school, gender disparities that tend to men are found to be more general, especially in the area of problem solving and application. However, these differences are not significant and gender differences can also be reduced over time. Recent findings relating to research on gender differences in mathematics, both in national and international studies, show that gender differences in mathematics have decreased year after year. The results of international comparative studies show that there are differences in mathematics learning outcomes between boys and girls in various countries. However, lately, the results of research on gender differences in mathematics show that there is no significant difference between men and women in terms of mathematical abilities. This happens along with the same treatment between men and women in the educational environment (Mullis, 2004). The results of the research described in this section show the diversity of research results regarding gender roles in mathematics learning. Some results

indicate the existence of gender factors in mathematics learning, but on the other hand, several studies reveal that gender does not have a significant effect on mathematics learning.

METHODOLOGY

Research methods can be interpreted as scientific procedures to obtain data with specific purposes and uses (Sugiyono, 2009). This study uses a mix method simultaneously to obtain a comprehensive analysis of research problems as stated by Creswell, (2013) or can be known as the concurrent mix method. This study uses research and development design, also known as R&D research. The results of this study are in the form of a Real Analysis course assessment instrument through the Rigorous Mathematical Thinking (RMT) approach based on gender.

Research Questions

From the explanation that has been explained in the introduction, then the formulation of the problem from this study are: (1) how to make an assessment prototype for the Real Analysis course?, (2) how to design an assessment instrument for Real Analysis?, (3) how to validate the instrument results assessment by expert validators, and (4) how the results test the effectiveness and practicality of the Real Analysis course assessment instruments that have been compiled. So the purpose of this study will be to produce an assessment prototype in the form of a valid, practical and effective course assessment instrument sheet for Real Analysis. aripemapan.

Modeling Volatility

The development model in this study will follow the steps of Borg and Gall (2003) which are more detailed and operational. The development model of Borg and Gall (2003) that should have been taken in development research has ten steps, but this research only reached the eighth step. The eight steps are: (1) preliminary study, (2) planning, (3) hypothetical model development, (4) hypothetical model review, (5) revision, (6) limited trial, (7) revision of trial results, (8) wider trial. This research only reached the eighth stage because this product was not to be tested en masse.

Data

Data collection techniques used are the method of written tests, documentation, observation, interviews, and questionnaires. Data analysis in the instrument development process, that is, the initial product is validated by the expert board to obtain valid instrument contents. Furthermore, this instrument was tested on a limited basis to the subject, namely FKIP UGJ students of mathematics education study program. The results of trial assessment instruments using the RMT approach based on gender are measured empirical validity using the product moment formula. While the reliability test uses alpha formula. The difficulty level of the question and the distinguishing force are also measured. In the instrument for evaluating democratic characters, the validity and reliability are measured using SPSS version 22 software.

RESULTS AND DISCUSSION

The results of the research related to the instruments used by researchers in measuring the ability of the RMT are carried out by written tests on material sequences and real functions. The

technique used by researchers in assessing aspects of mathematical thinking style is based on gender by making observations from the results of answers and lecture activities in the classroom and interview. The following is a question of RMT ability tests and then analyzed subject thinking styles based on gender.

No.	RMT Ability Test Questions for Sequence Materials and Real Functions
1.	Show that the sequence $(1+1/2!+1/3!+\dots+1/n!)$ is a Cauchy sequence and show that $(n+(-1)^n)/n$ is not a Cauchy sequence.
2.	Show if each sequence (x_n) and (y_n) is Cauchy, then (x_n+y_n) and $(x_n \cdot y_n)$ are also Cauchy.
3.	Show that the monotonically up and limited line is the Cauchy line.
4.	Suppose that (x_n) is a Cauchy sequence so that (x_n) is a sequence of integers for each natural number n . Show that the sequence (x_n) is finally constant.
5.	Suppose that y_1, y_2 is real number and $y_1 < y_2$. Define $y_n = 1/3y_{n-1} + 2/3y_{n-2}$ for $n > 2$. Show the sequence (y_n) convergent and specify the limit.

From the test questions above, the following is one of answers from classified subjects according to gender, namely men and women with random sampling techniques.

Question No.1

1) a) Barisan bil $(1+1/2! + \dots + 1/n!)$
 Misalkan $\epsilon > 0$ diberikan sebarang, pilih bilangan asli H sehingga $H - 2/\epsilon > 1$ jika $n, m > H$, maka $1/n! < \epsilon/2!$ dan $1/m! < \epsilon/2!$ oleh karena itu
 $|x_n - x_m| = |1/n! - 1/m!| < \epsilon/2! + \epsilon/2! = \epsilon$
 Karena $\epsilon > 0$ diberikan sebarang, maka dapat disimpulkan barisan (x_n) adalah barisan Cauchy
 b) Barisan $(1+(-1)^n/n)$ bukan barisan Cauchy
 Dari definisi barisan Cauchy, dapat ditunjukkan bahwa suatu barisan Cauchy jika dan hanya jika terdapat $\epsilon > 0$ sehingga untuk setiap bilangan asli H terdapat bilangan asli $n, m > H$ dan $|x_n - x_m| \geq \epsilon$
 Dari $x_n = 1 + (-1)^n/n$, jika n bilangan genap, maka $x_n = 1 + 1/n$ dan $x_{n+1} = 1 - 1/(n+1)$ jika diambil $\epsilon = 1/2$, maka untuk setiap bilangan asli H dapat dipilih suatu bilangan genap $n > H$ dan $n+1$ dan $|x_n - x_{n+1}| = 1/n + 1/(n+1) > 1/2 = \epsilon$
 Dari uraian diatas terbukti bahwa barisan (x_n) bukan barisan Cauchy.

Male Subject

1) a) Barisan bilangan $(1+1/2! + \dots + 1/n!)$
 Bukt: Misalkan $\epsilon > 0$ diberikan sebarang, pilih bilangan asli H sehingga $H - 2/\epsilon > 1$. Jika $n, m > H$, maka $1/n! < \epsilon/2!$ dan $1/m! < \epsilon/2!$ oleh karena itu
 $|x_n - x_m| = |1/n! - 1/m!| < \epsilon/2! + \epsilon/2! = \epsilon$
 Karena $\epsilon > 0$ diberikan sebarang, maka dapat disimpulkan barisan (x_n) adalah barisan Cauchy
 b) Barisan $(1+(-1)^n/n)$ bukan barisan Cauchy
 Dari definisi barisan Cauchy, dapat ditunjukkan bahwa suatu barisan Cauchy jika dan hanya jika terdapat $\epsilon > 0$ sehingga untuk setiap bilangan asli H terdapat bilangan asli $n, m > H$ dan $|x_n - x_m| \geq \epsilon$
 Dari $x_n = 1 + (-1)^n/n$, jika n bilangan genap, maka $x_n = 1 + 1/n$ dan $x_{n+1} = 1 - 1/(n+1)$ jika diambil $\epsilon = 1/2$, maka untuk setiap bilangan asli H dapat dipilih suatu bilangan genap $n > H$ dan $n+1$ dan $|x_n - x_{n+1}| = 1/n + 1/(n+1) > 1/2 = \epsilon$
 Dari uraian diatas terbukti bahwa barisan (x_n) bukan barisan Cauchy.

Female Subject

Question No.2

Misalkan $x^* = \sup \{x_n | n \in \mathbb{N}\}$ (Keberadaan x^* ini dijamin oleh karena 2.4.6)
 Selanjutnya akan ditunjukkan bahwa $x^* = \lim (x_n)$
 Jika diberikan sebarang $\epsilon > 0$ maka $x^* - \epsilon$ bukan batas atas dan $\exists x_k \in \mathbb{N}$
 Oleh karena itu terdapat $k \in \mathbb{N}$ sehingga $x_k - \epsilon < x_k$ tetapi karena (x_n) barisan naik, maka
 $x^* - \epsilon < x_k \leq x_n \leq x^*$; $\forall n \geq k$
 dan ini mengimplikasikan
 $|x_n - x^*| < \epsilon$; $\forall n \geq k$
 Karena $\epsilon > 0$ sebarang, maka $\lim (x_n) = x^*$ atau barisan (x_n) konvergen ke $x^* = \sup \{x_n | n \in \mathbb{N}\}$
 dan karena $\epsilon > 0$ diberikan sebarang, maka dapat disimpulkan barisan (x_n) konvergen ke $x^* = \sup \{x_n | n \in \mathbb{N}\}$ atau barisan Cauchy.

Male Subject

Tunjukkan jika (x_n) dan (y_n) masing-masing barisan Cauchy, maka $(x_n + y_n)$ dan $(x_n \cdot y_n)$ masing-masing barisan Cauchy.
 Jawab:
 a. Untuk $(x_n \cdot y_n)$
 $\{x_n\}$ dan $\{y_n\}$ adalah barisan Cauchy maka menurut 3.6.5 $\{x_n\}$ terbatas, yakni:
 $\exists \alpha, \beta > 0$ sehingga $|x_n| \leq \beta$ dan $|y_n| \leq \alpha, \forall n \in \mathbb{N}$
 $\{x_n\}$ barisan Cauchy $\Leftrightarrow \forall \epsilon > 0, \exists n_0 \in \mathbb{N} \exists \forall m, n \geq n_0$
 maka $|y_m - y_n| \leq \frac{\epsilon}{\alpha}$
 $\{y_n\}$ barisan Cauchy $\Leftrightarrow \forall \epsilon > 0, \exists n_0 \in \mathbb{N} \exists \forall m, n \geq n_0, |y_m - y_n| < \frac{\epsilon}{\alpha}$
 Akan ditunjukkan:
 $\{x_n \cdot y_n\}$ barisan Cauchy $\Leftrightarrow \forall \epsilon > 0, \exists n_0 \in \mathbb{N} \exists \forall m, n \geq n_0, |x_m \cdot y_m - x_n \cdot y_n| < \epsilon$
 Bukt:
 Misalkan sebarang $\epsilon > 0$ diberikan
 pilih $n_0 = \max \{n_1, n_2\}$ maka $\forall m, n \geq n_0$ berlaku
 $|x_m \cdot y_m - x_n \cdot y_n| = |x_m y_m - x_n y_m + x_n y_m - x_n y_n|$
 $\leq |x_m - x_n| |y_m| + |x_n| |y_m - y_n|$
 $< \frac{\epsilon}{2\alpha} \alpha + \frac{\epsilon}{2\alpha} \beta = \epsilon$

Female Subject

From the picture above, it can be seen that differences in thinking styles with the RMT approach will later be adjusted to gender. From the results of the answers, at first glance, there seems to be no difference in thinking style, but after being examined more deeply by interviewing each subject, there is a difference from the thinking style that is in accordance with his gender. The following are the results of the test for the ability of the RMT of line material and real functions with the product moment correlation that are made into table forms.

Table 2 Results of the RMT Ability Test for Sequence Materials and Real Functions

No.	NK	IV	TS	Validity	DR	TK	DP
1	0.640	High	$\alpha = 5\%$	Valid	High	Medium	2.905
2	0.425	Medium	$n = 15$	Valid	High	Medium	3.973
3	0.619	High	$r_{Tabel} =$	Valid	High	Medium	5.970
4	0.545	Medium	0.304	Valid	High	High	2.433
5	0.689	High	$r_{xy} > r_{Tabel}$	Valid	High	High	5.523

Keterangan :

- NK : Validity Correlation Score
- IV : Questions Validity Index
- TS : Questions Significance Level
- DR : Questions Reliability Degree
- TK : Questions Difficulty Level
- DP : Questions Differential Force

From the table above, it can be seen the results to prove the validity criteria, the degree of reliability of the question is calculated by alpha formula and the results obtained with high criteria and for the level of suitability of the problem depends on the medium and difficult region. After the validity test for ability test with RMT, below is a Real Analysis course assessment instrument with RMT adjusted for cognitive thinking style based on gender table.

From the table above, it can be seen that the assessment instrument for the Real Analysis course with the RMT approach adapted to the cognitive thinking style according to gender can represent the ability to think personally. So that this assessment instrument is expected to be able to raise the subject's learning achievements, especially the Real Analysis course. Because this instrument is so the basis for lecturers to provide lecture material by paying attention to aspects of cognitive thinking style according to gender that future expectations are subject learning achievement can increase optimally. This can be proven by the final value which shows the results with satisfying criteria. The following is a table of the results of the validity of the task assessment instrument and the results of the subject exam Real Analysis based on gender with the RMT approach.

Table 3 Assignment Assessment Instruments and Course Test Results of Real Analysis Based on Sex with the RMT Approach

Level	Cognitive Function	RMTIndicator	Cognitive thinking styles focused on sex		Scale			
			Male	Female	1	2	3	4
I	Qualitative Thinking	Labeling	√	√				
		Visualization	Spatial	Verbal				
		Comparison	Spatial	Verbal				
		Searching systematically to gather and complete information	√	√				
		Use of more than one source of information	√	√				
	Quantitative Thinking with Precision	Encoding Code solving	Spatial Spatial	Verbal Verbal				
		Preservation of provisions	Logic, reason and spatial	Logic, reason and verbal				
		Spatial measurement and relations	√	Not required				
		Analyzing	Logic, reason and spatial	Logic, reason, precision and verbal				
		Integration	Spatial	Verbal				
II	Abstract Relational Thinking	Generalization	Logic, reason and spatial	Logic, reason, precision and verbal				
		Previous mathematical knowledge activation	Spatial strategy	Verbal strategy				
		Logical mathematical evidence provision	√	√ (added verbal)				
		Articulating (pronunciation) logical mathematical events	√	√ (added verbal)				
		Defining the problem	Logic, reason and spatial	Logic, reason, precision and verbal				
	Relational Thinking	Generalization	Logic, reason and spatial	Logic, reason, precision and verbal				
		Hypothesis Thinking	Spatial	Verbal				
		Inferential Thinking	Spatial	Verbal				
		Relationship projecting and restructuring	Spatial strategy	Verbal strategy				
		Formation of proportional quantitative relations	Spatial strategy	Verbal strategy				
III	Abstract Relational Thinking	Mathematical inductive thinking	√	√				
		Mathematical deductive thinking	√	√				
		Mathematical relational thinking	√	√				
		Describing mathematical activities through cognitive categories	√	√				

Notes :
 √ = subjects are required to do so
 1 = Unable to do at all
 2 = Not able to do well
 3 = Enough to do well
 4 = Able to do very well

From the table above, it can be seen that the results of validity tests for task assessment instruments and course test results of Real Analysis based on gender with the RMT approach is valid with a medium to high validity index. The validity and reliability test of this instrument is conducted by an expert validator (rater) of two people who had doctoral degrees in mathematics education. Thus, the final conclusions from the validity and reliability test for this assessment instrument have a decent result or can be used properly.

Development of a course assessment prototype Real Analysis through a gender-based RMT approach is carried out with a preliminary study phase in order to establish and define the provisions when lecturing in class, as well as literature studies related to the problems studied to formulate a research framework. Activities carried out in this study include curriculum analysis, analysis of subject situations, lecture material analysis of Real Analysis, independent task analysis, and instructional objectives formulation.

Furthermore, questions about the ability of the RMT are made to measure the subject cognitive abilities and test the validity, reliability and index of the difficulties first. After that, a Real Analysis course assessment instrument is created, which is focused on gender-thinking cognitive styles.

The practicality of the developed prototype assessment of the Real Analysis course can be determined by the following indicators: 1) the use of lecture devices; 2) the observations results of the lecturers ability in managing lectures using assessment instruments in very good categories; 3) subject response to positive lecture ratings, indicated by a percentage more than 80% (Amidi 2012: 106). The results of the developed course assessment prototype usage of Real Analysis can be seen from the total average value of all meetings. The average total use of the developed prototype assessment of the Real Analysis course is 3.98, so it is concluded that the use of prototypes is in the category of "good". The results of the researchers' responses in using lecture assessment instruments of Real Analysis are obtained a total average of two raters, namely 85. This means that the use of the developed prototype is classified as "very good". While the subject response showed positive results, the course assessment prototype of Real Analysis with the RMT approach based on gender is said to be practical. The test results of the course assessment prototype effectiveness of Real Analysis with the RMT approach based on gender can be seen if the assessment instrument meets the criteria of valid, reliable, objective, systematic, economical, and practical (Sudiyatno 2010: 239). In general, the rater assesses that the prototype assessment course of Real Analysis with a gender-based RMT approach

has a very good value of objectivity, economics and systematic.

The subject also give a positive response, as indicated by the results of a questionnaire that shows interest in joining the next

Table 4 Validity Test Results of Assignment Assessment Instruments and Course Test Results of Real Analysis Based on Gender with the RMT Approach

BP	Indikator RMT	NV	IV	NR	IR
1	Labeling	0.728	High		
2	Visualization	0.831	High		
3	Comparison	0.670	High		
4	Searching systematically to gather and complete information	0.827	High		
5	Use of more than one source of information	0.561	Medium		
6	Encoding	0.680	High		
7	Code solving	0.773	High		
8	Preservation of provisions	0.811	High		
9	Spatial measurement and relations	0.731	High		
10	Analyzing	0.570	Medium		
11	Integration	0.628	High	R ₁₁ = 0.755	
12	Generalization	0.640	High		
13	Previous mathematical knowledge activation	0.510	Medium	So that it can	
14	Logical mathematical evidence provision	0.487	Medium	:	High
15	Articulating (pronunciation) logical mathematical events	0.428	Medium		
16	Defining the problem	0.528	Medium	0.60 <	
17	Generalization	0.613	High	R ₁₁ < 0.80	
18	Hypothesis Thinking	0.788	High		
19	Inferential Thinking	0.630	High		
20	Relationship projecting and restructuring	0.597	Medium		
21	Formation of proportional quantitative relations	0.778	High		
22	Mathematical inductive thinking	0.690	High		
23	Mathematical deductive thinking	0.528	Medium		
24	Mathematical relational thinking	0.647	High		
25	Descripting mathematical activities through cognitive categories	0.638	High		

Keterangan :
 BP : Butir Pengamatan (Observation Item)
 NV : Nilai Validitas (Validity Score)
 IV : Indeks Validitas (Validity Index)
 NR : Nilai Reliabilitas (Reliability Value)
 IR : Indeks Reliabilitas (Reliability Index)

It is illustrated by the average for each aspect, namely Objectivity 3.56 (very good), 3.45 (very good) and Systematic 3.56 (very good), while the validity, reliability and practicality have also been tested. Overall, it can be concluded that the effectiveness criteria have been fulfilled.

CONCLUSIONS AND RECOMMENDATIONS

Based on the results of research and discussion, it can be concluded as follows: (1) The lecturer has not so fully used the Real Analysis course assessment prototype with a gender-based RMT approach that it is expected that in the future it can use and assess the subject's cognitive abilities more fairly and measurably, (2) development of a course assessment prototype of Real analysis with a gender-based RMT approach produces valid, reliable, practical and effective assessment instruments, (3) the results of the trial of prototype assessment course of Real Analysis with the RMT approach based on gender are measured empirical validity using the product moment formula which produces 5 items declared valid. For reliability test, the researcher uses alpha formula with results of the assessment prototype having a high degree of reliability. The difficulty level is balanced, where there are difficult and moderate questions. As for the differentiating force, the results of the test questions can distinguish between high, medium and low ability subjects. Positive responses from interested lecturers in using a course assessment prototype of Real analysis with a gender-based RMT approach provide excellent comments on the assessment instruments that have been prepared. Based on the results of observations of lecture management capabilities, the researcher obtains scores from a maximum score of 36.

The developed course assessment prototype of Real analysis with a gender-based RMT approach was is effective. It is indicated by the fulfillment of valid, reliable, objective, systematic, economical, practical and effective criteria with an average score obtained at 3.54 which means the product effectiveness is very high.

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